NAME: ID:

$Math\ 317\ Q1\ Winter\ 2017\ Quiz\ 6$

Apr. 7, 2017, 25 minutes

• The quiz has 3 problems. Total 10 + 1 points.

QUESTION 1. (5 PTS) Let $f(x) := \sum_{n=0}^{\infty} (-1)^n \frac{x^{2n+1}}{2n+1}$. Determine the domain of f and obtain an explicit formula for f. Justify your calculation.

QUESTION 2. (5 PTS) Calculate the Fourier series for the function $f(x)=\begin{cases} -\pi & -\pi < x < 0 \\ x & 0 < x < \pi \end{cases}$.

QUESTION 3. (1 BONUS PT) Find the sum $\sum_{n=1}^{\infty} \frac{1}{n^2+1}$ by considering the Fourier series of e^{-x} .