Challenge Problem

Show that every simple graph contains two nodes of equal degree. A graph is *simple* if it does not have loops and multiple edges.
Challenge Problem

Show that if a simple graph has $n$ nodes, each of degree at least $(n - 1)/2$, then the graph is connected. A graph is *simple* if it does not have loops and multiple edges.