Midpoint rule is a numerical integrator for ordinary differential equations. When used to simulate mechanical systems, it may reveal various structure-preserving features, such as symplecticity. The talk will discuss the variational origins and structure-preserving properties of this integrator when calculations are carried out relative to a moving frame. Numerical simulations of skate's dynamics and rotating controlled rigid body will illustrate the theory.