MATH 214 (R1) Winter 2008 Intermediate Calculus I



Problem Set #8

Completion Date: Friday March 14, 2008

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Question 1. [Sec. 13.4, # 16] Find two unit vectors orthogonal to both i + j + k and 2i + k.

Question 2. [Sec. 13.4, # 24] Find the area of the parallelogram with vertices K(1, 2, 3), L(1, 3, 6), M(3, 8, 6), and N(3, 7, 3).

Question 3. [Sec. 13.4, # 28] Given the points P(2, 0, -3), Q(3, 1, 0), and R(5, 2, 2),

- (a) find a vector orthogonal to the plane through the points P, Q, and R, and
- (b) find the area of triangle $\triangle PQR$.

Question 4. [Sec. 13.4, # 32] Given the points

 $P(0,1,2), \quad Q(2,4,5), \quad R(-1,0,1), \quad S(6,-1,4),$

find the volume of the parallelopiped with adjacent edges PQ, PR, and PS.

Question 5. [Sec. 13.5, # 10] Find parametric equations and symmetric equations for the line through the point (2, 1, 0) and perpendicular to both $\mathbf{i} + \mathbf{j}$ and $\mathbf{j} + \mathbf{k}$.

Question 6. [Sec. 13.5, # 16]

- (a) Find parametric equations for the line through (5, 1, 0) that is perpendicular to the plane 2x y + z = 1.
- (b) In what points does this line intersect the coordinate planes?

Question 7. [Sec. 13.5, # 24] Find an equation of the plane through the point (4, 0, -3) and with normal vector $\mathbf{j} + 2\mathbf{k}$.

Question 8. [Sec. 13.5, # 34] Find an equation of the plane that passes through the point (1, 2, 3) and contains the line

$$x = 3t$$
, $y = 1 + t$, $z = 2 - t$, $-\infty < t < \infty$.

Question 9. [Sec. 13.5, # 46] Given the planes

2z = 4y - x and 3x - 12y + 6x = 1,

determine whether the planes are parallel, perpendicular, or neither. If neither, find the angle between them.

Question 10. [Sec. 13.5, # 54] Find parametric equations for the line of intersection of the planes

2x + 5z + 3 = 0 and x - 3y + z + 2 = 0.

Question 11. [Sec. 14.1, # 4] Find the limit

$$\lim_{t \to 0} \left\langle \frac{e^t - 1}{t}, \frac{\sqrt{1 + t} - 1}{t}, \frac{3}{1 + t} \right\rangle.$$

Question 12. [Sec. 14.1, # 12] Sketch the curve with vector equation

$$\mathbf{r}(t) = t\,\mathbf{i} + t\,\mathbf{j} + \cos t\,\mathbf{k}.$$

Indicate with an arrow the direction in which t increases.

Question 13. [Sec. 14.1, # 14] Sketch the curve with vector equation

$$\mathbf{r}(t) = \sin t \, \mathbf{i} + \sin t \, \mathbf{j} + \sqrt{2} \cos t \, \mathbf{k}.$$

Indicate with an arrow the direction in which t increases.

Question 14. [Sec. 14.1, # 18] Given the points P(-2, 4, 0) and Q(6, -1, 2), find a vector equation and parametric equations for the line segment that joins P to Q.

Question 15. [Sec. 14.1, # 34] Find a vector function that represents the intersection of the following surfaces: the cylinder $x^2 + y^2 = 4$ and the surface z = xy.