### Linear Analysis

#### Math 516 – Lecture A1

## September – December 2007

Time and Place: TR 9:30 – 10:50, CAB 563.

Instructor: Alexander Litvak

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Homepage: http://www.math.ualberta.ca/~alexandr/

Office Hours: TBA

### Recommended books (no textbook needed):

1. B. Bollobas, Linear Analysis. *An Introductory Course*, Second Edition. Cambridge University Press, 1999.

- 2. J.B. Conway, A Course in Functional Analysis, Springer Verlag, 1985.
- 3. N. Dunford and J.T. Schwartz, Linear Operators, I. Wiley-Interscience, 1988.
- 4. M. Fabian, P. Habala, P. Hajek, V. Montesinos, J. Pelant and V. Zizler, Functional Analysis and Infinite dimensional Geometry, Canad. Math. Soc. Books in Math. 8 (Springer-Verlag 2001).
- 5. L.V. Kantorovich, G.P. Akilov, *Functional analysis*, Translated from the Russian by Howard L. Silcock. Second edition. Pergamon Press, Oxford-Elmsford, N.Y., 1982.
- 6. W. Rudin, Functional Analysis, Second Edition. McGraw-Hill, 1991.
- 7. V. Runde, *Math 516 Linear Analysis*, Lecture notes, http://www.math.ualberta.ca/~runde/math516.html.

Prerequisite: Math 418 or equivalent.

# Topics to be covered:

- 1. Normed spaces and Banach spaces;
- 2. The principles of functional analysis: the Hahn-Banach theorem, the uniform boundedness principle (the Banach-Steinhaus theorem), the open mapping theorem, the closed graph theorem;
- 3. Hilbert spaces and orthonormal bases;
- 4. Spectral theory of compact normal operators;
- 5. Fixed point theorems with applications.

### **Grading Policy:**

Your course grade will be based upon your marks in examinations and assignments weighted as follows:

50% Final (09:00–12:00, CAB 563, Monday, December 17) 30% Midterm (9:30–10:50, CAB 563, Thursday, November 1)

20% Assignments

There is no deferred midterm. If you qualify for an excused absence on a midterm the weight will be transferred to the final exam. If you miss the final exam and obtain a formal (in writing) University accepted excuse for your absence you might write a **deferred exam**.

Assignments: Homework problems will be assigned in every lecture and all the problems assigned in the current week will be due at the **beginning** of the Thursday class of the next week in the lecture room CAB 563. Please note, late assignments will not be accepted. The solutions will be posted at my homepage. I strongly recommend that you do all the drill problems that will be recommended each week together with the assignment.

**Dates:** First Class: Sept. 6; Midterm exam: Nov. 1; Fall term class break: Nov. 13 (no classes are held); Last class: Dec. 4; Final exam: Dec. 17; Deferred exam: TBA.

#### Additional announcement:

As usual there will be Functional Analysis Seminar this year. If you are interested in participating, could you please provide me your schedule and e-mail address, so we could find time convenient to everybody.