Linear Analysis

Math 516 - Lecture A1

September – December 2006

Time and Place: TR 9:30 – 10:50, CAB 657.

Instructor: Alexander Litvak

Office: CAB 525, tel: 492-3397, e-mail: alexandr@math.ualberta.ca Homepage: http://www.math.ualberta.ca/~alexandr/ Office Hours: TR 11:00-12:00 or by appointment.

Recommended books (no textbook needed):

1. B. Bollobas, Linear Analysis. An Introductory Course, Second Edition. Cambridge University Press, 1999.

2. J.B. Conway, A Course in Functional Analysis, Springer Verlag, 1985.

3. N. Dunford and J.T. Schwartz, *Linear Operators*, I. Wiley-Interscience, 1988.

4. M. Fabian, P. Habala, P. Hajek, V. Montesinos, J. Pelant and V. Zizler, *Functional Analysis and Infinite dimensional Geometry*, Canad. Math. Soc. Books in Math. 8 (Springer-Verlag 2001).

5. L.V. Kantorovich, G.P. Akilov, *Functional analysis*, Translated from the Russian by Howard L. Silcock. Second edition. Pergamon Press, Oxford-Elmsford, N.Y., 1982.

6. W. Rudin, *Functional Analysis*, Second Edition. McGraw-Hill, 1991.

7. V. Runde, Math 516 - Linear Analysis, Lecture notes,

http://www.math.ualberta.ca/~runde/math516.html.

Prerequisite: Math 418 or equivalent.

Topics to be covered:

1. Normed spaces and Banach spaces;

2. The principles of functional analysis: the Hahn-Banach theorem, the uniform boundedness principle (the Banach-Steinhaus theorem), the open mapping theorem, the closed graph theorem;

3. Hilbert spaces and orthonormal bases;

4. Spectral theory of compact normal operators;

5. Fixed point theorems with applications.

Grading Policy:

Your course grade will be based upon your marks in examinations and assignments weighted as follows:

- 50% Final (09:00–12:00, CAB 657, Friday, December 15)
- 30% Midterm (9:30–10:50, CAB 657, Thursday, October 26)

20% Assignments

There is no deferred midterm. If you qualify for an excused absence on a midterm the weight will be transferred to the final exam. If you miss the final exam and obtain a formal (in writing) University accepted excuse for your absence you might write a **deferred exam** on Saturday, **January 13, 2007** at 9:00–12:00 in CAB 243.

Assignments: Homework problems will be assigned in every lecture and all the problems assigned in the current week will be due at the **beginning** of the Thursday class of the next week in the lecture room CAB 657. **Please note**, late assignments will not be accepted. **The solutions** will be posted at my homepage. I **strongly recommend** that you do all the drill problems that will be recommended each week together with the assignment.

Dates: First Class: Sept. 7; Midterm exam: Oct. 26; Fall term class break: Nov. 14 (no classes are held); Last class: Dec. 5; Final exam: Dec. 15; Deferred exam: Jan. 13.

Additional announcements:

1. As usual there will be Functional Analysis Seminar this year. If you are interested in participating, could you please provide me your schedule and e-mail address, so we could find time convenient to everybody.

2. The following course could be interesting for you:

Fall 2006: "Measure Theory" (MATH 543) by V. Runde.