# Linear Analysis

# Math 516 - Lecture A1

### September – December 2005

Time and Place: TR 9:30 – 10:50, CAB 657.

#### Instructor: Alexander Litvak

Office: CAB 525, tel: 492-3397, e-mail: alexandr@math.ualberta.ca Homepage: http://www.math.ualberta.ca/~alexandr/ Office Hours: TR 11:00-12:00 or by appointment.

### Recommended books (no textbook needed):

1. B. Bollobas, Linear Analysis. An Introductory Course, Second Edition. Cambridge University Press, 1999.

2. J.B. Conway, A Course in Functional Analysis, Springer Verlag, 1985.

3. N. Dunford and J.T. Schwartz, *Linear Operators*, I. Wiley-Interscience, 1988.

4. M. Fabian, P. Habala, P. Hajek, V. Montesinos, J. Pelant and V. Zizler, *Functional Analysis and Infinite dimensional Geometry*, Canad. Math. Soc. Books in Math. 8 (Springer-Verlag 2001).

5. L.V. Kantorovich, G.P. Akilov, *Functional analysis*, Translated from the Russian by Howard L. Silcock. Second edition. Pergamon Press, Oxford-Elmsford, N.Y., 1982.

6. W. Rudin, *Functional Analysis*, Second Edition. McGraw-Hill, 1991.

7. V. Runde, Math 516 - Linear Analysis, Lecture notes,

http://www.math.ualberta.ca/~runde/math516.html.

Prerequisite: Math 418 or equivalent.

# Topics to be covered:

1. Normed spaces and Banach spaces;

2. The principles of functional analysis: the Hahn-Banach theorem, the uniform boundedness principle (the Banach-Steinhaus theorem), the open mapping theorem, the closed graph theorem;

3. Hilbert spaces and orthonormal bases;

4. Spectral theory of compact normal operators;

5. Fixed point theorems with applications.

# Grading Policy:

Your course grade will be based upon your marks in examinations and assignments weighted as follows:

- 50% Final (09:00–12:00, CAB 657, Thursday, December 15)
- 30% Midterm (9:30–10:50, CAB 657, Thursday, October 27)

20% Assignments

There is no deferred midterm. If you qualify for an excused absence on a midterm the weight will be transferred to the final exam. If you miss the final exam and obtain a formal (in writing) University accepted excuse for your absence you might write a **deferred exam** on Saturday, **January 14, 2006** at 9:00–12:00 in CAB 243.

Assignments: Homework problems will be assigned in every lecture and all the problems assigned in the current week will be due at the **beginning** of the Thursday class of the next week in the lecture room CAB 657. Please note, late assignments will not be accepted. The solutions will be posted at my homepage as well as on Bulletin board # 9b, opposite CAB 529. I strongly recommend that you do all the drill problems that will be recommended each week together with the assignment.

**Dates:** First Class: Sept. 8; Midterm exam: Oct. 27; Fall term class break: Nov. 10 (no classes are held); Last class: Dec. 6; Final exam: Dec. 15; Deferred exam: Jan. 14.

#### Additional announcement:

As usual there will be Functional Analysis Seminar this year. If you are interested in participating, could you please provide me your schedule and e-mail address, so we could find time convenient to everybody.