

for a medium box, and \$4.50 for a large box. Fixed costs are \$8000.

(a) Express the cost of making  $x$  small boxes,  $y$  medium boxes, and  $z$  large boxes as a function of three variables:  
 $C = f(x, y, z)$ .

(b) Find  $f(3000, 5000, 4000)$  and interpret it.

(c) What is the domain of  $f$ ?

9. Let  $g(x, y) = \cos(x + 2y)$ .

(a) Evaluate  $g(2, -1)$ .

(b) Find the domain of  $g$ .

(c) Find the range of  $g$ .

10. Let  $F(x, y) = 1 + \sqrt{4 - y^2}$ .

(a) Evaluate  $F(3, 1)$ .

(b) Find and sketch the domain of  $F$ .

(c) Find the range of  $F$ .

11. Let  $f(x, y, z) = \sqrt{x} + \sqrt{y} + \sqrt{z} + \ln(4 - x^2 - y^2 - z^2)$ .

(a) Evaluate  $f(1, 1, 1)$ .

(b) Find and describe the domain of  $f$ .

12. Let  $g(x, y, z) = x^3 y^2 z \sqrt{10 - x - y - z}$ .

(a) Evaluate  $g(1, 2, 3)$ .

(b) Find and describe the domain of  $g$ .

13–22 Find and sketch the domain of the function.

13.  $f(x, y) = \sqrt{2x - y}$

14.  $f(x, y) = \sqrt{xy}$

15.  $f(x, y) = \ln(9 - x^2 - 9y^2)$

16.  $f(x, y) = \sqrt{x^2 - y^2}$

17.  $f(x, y) = \sqrt{1 - x^2} - \sqrt{1 - y^2}$

18.  $f(x, y) = \sqrt{y} + \sqrt{25 - x^2 - y^2}$

19.  $f(x, y) = \frac{\sqrt{y - x^2}}{1 - x^2}$

20.  $f(x, y) = \arcsin(x^2 + y^2 - 2)$

21.  $f(x, y, z) = \sqrt{1 - x^2 - y^2 - z^2}$

22.  $f(x, y, z) = \ln(16 - 4x^2 - 4y^2 - z^2)$

23–31 Sketch the graph of the function.

23.  $f(x, y) = 1 + y$

24.  $f(x, y) = 2 - x$

25.  $f(x, y) = 10 - 4x - 5y$

26.  $f(x, y) = e^{-y}$

27.  $f(x, y) = y^2 + 1$

28.  $f(x, y) = 1 + 2x^2 + 2y^2$

29.  $f(x, y) = 9 - x^2 - 9y^2$

30.  $f(x, y) = \sqrt{4x^2 + y^2}$

31.  $f(x, y) = \sqrt{4 - 4x^2 - y^2}$

32. Match the function with its graph (labeled I–VI). Give reasons for your choices.

(a)  $f(x, y) = |x| + |y|$

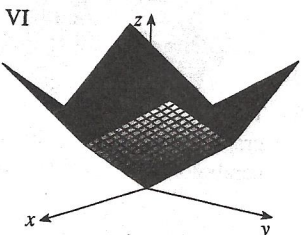
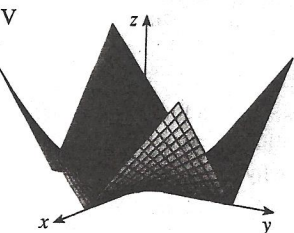
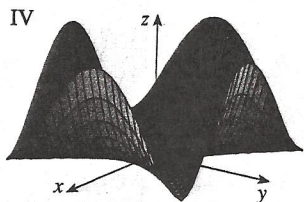
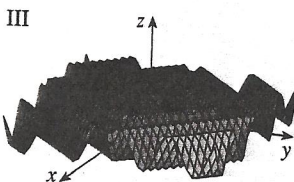
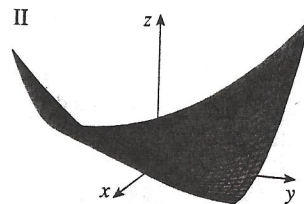
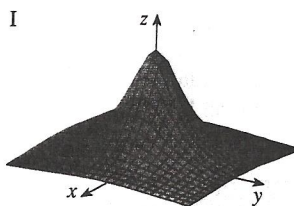
(b)  $f(x, y) = |xy|$

(c)  $f(x, y) = \frac{1}{1 + x^2 + y^2}$

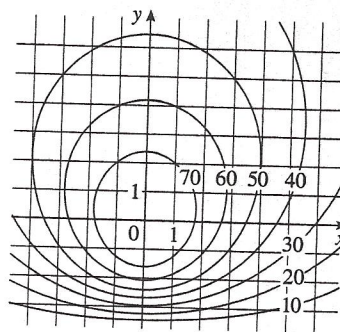
(d)  $f(x, y) = (x^2 - y^2)^2$

(e)  $f(x, y) = (x - y)^2$

(f)  $f(x, y) = \sin(|x| + |y|)$



33. A contour map for a function  $f$  is shown. Use it to estimate the values of  $f(-3, 3)$  and  $f(3, -2)$ . What can you say about the shape of the graph?



34. Shown is a contour map of atmospheric pressure in North America on August 12, 2008. On the level curves (called isobars) the pressure is indicated in millibars (mb).

(a) Estimate the pressure at  $C$  (Chicago),  $N$  (Nashville),  $S$  (San Francisco), and  $V$  (Vancouver).

(b) At which of these locations were the winds strongest?

