Problem 1. a. Given sets A and B define $A \setminus B$ and $A \cap B$.

b. Let $A = \{\emptyset, a, b, \{1\}, x\}$ and $B = \{a, 1, x\}$. Find $A \setminus B$ and $A \cap B$.

Solution. a.

$$A \setminus B = \{x \mid x \in A \text{ and } x \notin B\},$$
 $A \cap B = \{x \mid x \in A \text{ and } x \in B\}.$

b.

$$A \setminus B = \{\emptyset, b, \{1\}\}, \qquad \qquad A \cap B = \{a, x\}.$$

Problem 2. Let P,Q be statements. Provide truth tables for $(P\Rightarrow Q), (P \text{ and } Q), (P \text{ or } Q),$ not P.

Solution. See the attached table. Note that we used that

$$(P \Rightarrow Q) = ((\text{not } P) \text{ or } Q).$$