## Math 421 Q1 Winter 2017 Homework 1

Due Jan. 19, 12pm.

Total 20 points.

QUESTION 1. (5 PTS) A committee is to be chosen from among 8 scientists, 7 psychics, and 12 clerics. If the committee is to have two members of different backgrounds, how many such committees are there? Justify your answer.

QUESTION 2. (5 PTS) How many 5-letter words<sup>1</sup> either start with d or do not have the letter d? Justify your answer.

QUESTION 3. (5 PTS) In how many ways can we get a sum of 4 when two dice are rolled if the two dice are identical. Justify your answer.

QUESTION 4. (5 PTS) A composition of a positive integer n is an ordered list of positive integers (called parts) that sum to n. The four compositions of 3 are 3; 2,1; 1,2 and 1,1,1. Obtain a formula for the number of compositions of n. Justify your answers.

<sup>1.</sup> a "5-letter word" here just means an ordered list of 5 letters. For example abcde is a word.